ABSTRACT: Granular pile anchor foundations (GPAF) are a promising foundation system that can be used to mitigate the serious consequences of volumetric changes of reactive soils, both during expansion and shrinkage. This paper presents results from 3D finite element analyses, using PLAXIS software, undertaken on a typical double-story building constructed over a system of GPAF in a reactive soil. The study investigates the ability of the GPAF system to resist the forces induced by soil movement due to moisture variation, and the impact of this resistance on the straining actions affecting the superstructure. The results confirm the efficiency of the GPAF system in arresting the movement of the reactive soil, which in turn improves the structural responses of the building in terms of induced deformations, angular distortions and internal forces.

1. INTRODUCTION
Reactive soils are clays that swell and shrink with changing moisture content, and are found in many arid and semiarid regions around the world. For example, it is estimated that 20% of the Australian surface soil can be classified as reactive [1]. There are several factors that influence the swelling and shrinking potential of clay soils, including the amount and type of clay minerals, cation exchange capacities, availability of moisture and the initial water content. The swell/shrink ground movements associated with reactive soils pose significant challenge to the geotechnical community as they cause distress to foundations of lightweight structures and cracking in retaining walls, pavements, canal beds and linings [2, 3].

Despite the numerous foundation systems that have been developed over the past decades to control the movements induced by reactive soils, substantial financial losses are still incurred every year in many places around the world. For example, the American Society of Civil Engineers estimated that about one quarter of all homes in the US have experienced some damage from reactive soils; the financial losses incurred by property owners exceed those caused by natural disasters such as earthquakes, floods, hurricanes and tornadoes combined [4]. In Australia, and despite the stringent regulatory requirements, most of the lightweight buildings constructed on reactive soils experience some distortional damage during their early lives [5].

The literature includes numerous solutions for construction on reactive soils, including replacement of the entire reactive material, pile foundations [6], soil stabilization using additives [7, 8], and implementation of special types of foundations such as drilled and friction piers [3]. One promising, special foundation solution that has been recently proposed is the granular pile anchor foundation (GPAF). The GPAF is an innovative technique that has shown great potential as a solution to founding structures safely into reactive soils. The GPAF system was first proposed by Phanikumar and Ramachandra Rao [9] for reactive soils under heave conditions and was later pursued by other investigators [e.g. 10, 11] via laboratory and field trials. In an attempt to determine the controlling parameters of the GPAF technique to resist the heave and shrinkage induced by reactive soils, the efficiency of the technique was further investigated numerically by Ismail and Shahin [12] using the finite element method (FEM). Despite the success of the GPAF reported by the above investigators, it is yet to be applied in practice, primarily due to the limited field trials.

In this paper, the performance of the GPAF system under heave and shrinkage is investigated by 3D numerical analysis for a typical double-story, four-bay structure founded in reactive soil. The investigation explored the efficiency of the system in arresting the ground movements induced by soil heave/shrinkage, and the implications of this on the internal forces experienced by the superstructure.

2. CONCEPT OF GPAF SYSTEM
Fig. 1 shows the concept of the GPAF system, which is a hybrid solution in which a shallow foundation is supported on a granular pile that derives its resistance from the interface between the granular pile and surrounding reactive soil.
As can be seen in Fig. 1, a typical GPAF system consists of a pile of granular material installed into the reactive soil. A concrete footing is then constructed above the granular pile and connected to it via a steel anchor that is monolithically casted with the concrete footing to transfer the load between the footing and the pile. The uplift resistance is mobilized as skin friction along the periphery of the granular pile at its interface with the surrounding soil. The force in the pile anchor is transmitted to this interface via a base plate that is rigidly connected to the pile anchor. According to this arrangement of the anchorage system between the footing and granular pile, the latter cannot only reinforce the ground (as in the case of soft clay and loose sand) but can also effectively resist the uplift forces from an expansive soil. As can be inferred from Fig. 1, the uplift resistance of the GPAF system is a function of the self-weight of the pile-footing assembly, interface shear strength, surface area of the granular pile and normal stress developed during expansion of the soil surrounding the pile. In the experiment performed by Phanikumar et al. [13], the undrained shear strength of the expansive clay surrounding the granular pile was shown to have increased by about 20%, compared with the clay in the free field zone due to the expansion-induced normal stresses.

3. NUMERICAL ANALYSES OF TWO-STORY BUILDING RESTING ON GPAF SYSTEM

In order to investigate the efficiency of the GPAF system in practice, a two-story four-bay frame building resting on a system of GPAF is considered in the current study. The problem is analyzed by numerical modeling using the commercially available finite element software PLAXIS 3D Foundation [14].

3.1 Problem Identification

The two-story frame building considered in the current study is 6 m high (each story is 3 m in height), and is 20 m × 20 m in plan with each bay having dimensions of 5 m × 5 m. A ceiling slab of 160 mm thick is assumed for each story. The slabs are supported by beams, 300 mm wide and 400 mm deep, which in turn rest on square columns of dimensions 300 mm × 300 mm. The dead load of each structural component of the frame building is considered according to the material unit weight of that component, and an additional distributed live load of 5 kPa is also assumed to act on top of the slabs. All concrete materials (including footings) are made of concrete of an elastic modulus of 35 GPa, Poisson’s ratio of 0.2 and unit weight of 24 kN/m³.

The GPAF system consists of square pad footings of dimensions 2 m × 2 m, each supported on a group of three granular piles of 0.5 m in diameter and 3.0 m in length. A schematic diagram of the arrangement of the three granular piles within the pad footing is shown in Fig. 2. A group of piles is used rather than a single pile to enhance the rotational stiffness and stability of the system. The problem is analyzed using the 3D model presented in Fig. 3, which has a discretized mesh that consists of 17,880 wedge elements of 15 displacement nodes and 6 Gaussian stress points each.
The idealized ground profile consists of a gently sloping reactive clay layer of an average thickness of 3.5 m (across the footing footprint) overlying dense sand of an average thickness of 11.5 m. The model is strategically refined around the footing and granular piles to improve the accuracy of the analysis and the boundaries are located farther from the area of interest to minimize the boundary effect. The concrete footings are located 1.0 m below the ground surface and are modeled using a Mindlin’s plate element of thickness of 0.6 m. The pile anchor is modeled as an elastic embedded pile of 75 mm in diameter with an elastic modulus of 200 GPa. The steel base plate is modeled as an infinitely rigid plate. All pad footings are connected by concrete tie beams (see Fig. 3b), 300 mm wide and 600 mm deep.

3.2 Soil Models and Parameters

The reactive clay is modeled using a Mohr-Coulomb (MC) model and is assumed to behave in a drained manner during expansion and shrinking. The underlying dense sand and granular pile material are best modeled using the hardening soil constitutive model (HS). The HS model [15] is a non-linear elastic plastic formulation which adopts multiple yield loci as a function of plastic shear strain and a cap to allow volumetric hardening. The non-linear stress strain relationship is represented by a hyperbolic formula, with primary loading governed by a secant deformation modulus \( E_{50} \) at 50% of the material strength. Loading and unloading within the current yield surface are assumed to be elastic (defined by a separate modulus, \( E_{ur} \)) with failure governed by the Mohr-Coulomb failure criterion. Both \( E_{50} \) and \( E_{ur} \) evolve with the minor effective stress, \( \sigma_3' \), according to the following formula:

\[
E_{50} = E_{50}' \left( \frac{c \cos \phi - \sigma_3' \sin \phi}{c \cos \phi + p_{ref} \sin \phi} \right)^m
\]

(1)

where: \( c \) is the soil effective cohesion, \( \phi \) is the effective peak friction angle, \( m \) is the exponent that controls the dependency of the stiffness on stress and \( p_{ref} \) is the reference stress corresponding to \( E_{50}' \). A summary of the material parameters used for all soils are presented in Table 1. It should be noted that the properties of the reactive clay are those evolving after the wetting/drying event and during expansion/shrinking. In reality, the strength of a reactive soil degrades during expansion and increases during shrinking (due to suction), but this is not modeled in this study.

The rate of volume change at which reactive clays would normally encounter depends on the location from the source of moisture and magnitude of overburden pressure. In the current study, a leaking event of an underground water facility located underneath the central column is assumed to cause arbitrary values of heave and shrinkage of 20% and 10%, respectively, over the layer thickness of the affected area underneath the central footing, as shown in Fig. 3b. Both heave and shrinkage were modeled by applying equivalent volumetric strains to the affected area. The heave and shrinkage events are applied independent of each other, starting from the stage after application of the dead and live loads.

Table 1. Soil properties used in the finite element analyses

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Reactive Clay</th>
<th>Dense Sand</th>
<th>Granular Pile</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \gamma ) (kN/m(^3)) ^(1)</td>
<td>15</td>
<td>20</td>
<td>20</td>
</tr>
<tr>
<td>( E_{50}' ) (MPa)</td>
<td>2</td>
<td>75</td>
<td>200</td>
</tr>
<tr>
<td>( E_{ur}' ) (MPa)</td>
<td>–</td>
<td>75</td>
<td>200</td>
</tr>
<tr>
<td>( c ) (kPa)</td>
<td>2</td>
<td>0.1</td>
<td>0.1</td>
</tr>
<tr>
<td>( \phi ) (°)</td>
<td>24</td>
<td>36</td>
<td>40</td>
</tr>
<tr>
<td>( v_{ur} ) ^(2)</td>
<td>0.35</td>
<td>0.2</td>
<td>0.2</td>
</tr>
<tr>
<td>( \rho_{ref} ) (kPa)</td>
<td>–</td>
<td>100</td>
<td>100</td>
</tr>
<tr>
<td>( m )</td>
<td>–</td>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>( K^0 ) ^(3)</td>
<td>0.6</td>
<td>0.4</td>
<td>0.4</td>
</tr>
</tbody>
</table>

\(^{1}\) Soil unit weight; \(^{2}\) Unload-reload Poisson’s ratio; \(^{3}\) Coefficient of earth pressure at rest.

4. RESULTS AND DISCUSSION

In order to investigate the efficiency of the GPAF system in enhancing the behavior of the two-story building constructed over a reactive soil, an additional independent analysis is carried out for the building resting on pad footings without the GPAF and the results are compared with those obtained from the analysis of the building resting on the GPAF system. The comparison is made for the top beams of the central frame (i.e. beams B1 to B4 in Fig. 4). The comparison results in terms of induced deformations due to heave and shrinkage are shown in Fig. 5, and the angular distortions and bending moments due to heave are given in Table 2.

![Fig. 4: Schematic diagram of the central frame](image)

It can be seen from Fig. 5 that the ability of the pad footings to resist the vertical movements induced by soil heave is significantly improved when the GPAF system is used. The maximum vertical displacement induced by soil heave for
beams B1–B4 without the GPAF system is found to be equal to 6.7 mm, whereas negligible vertical movement is developed when the GPFA system is used. More importantly, it can be seen from Table 2 that all beams undergo much less angular distortions when the GPFA system is used. For example, the angular distortion of beam B2 without the GPFA system is some 300 times greater than that experienced when the GPFA system is used.

Table 2. Angular distortions and internal forces of central beams B1 to B4 due to heave

<table>
<thead>
<tr>
<th>Beam Number</th>
<th>Angular distortion ($\times 10^{-5}$)</th>
<th>Maximum negative moment (kN.m)</th>
<th>Maximum positive moment (kN.m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>B1</td>
<td>GPAF 0.6</td>
<td>44.6</td>
<td>23.0</td>
</tr>
<tr>
<td></td>
<td>No GPAF 50</td>
<td>81.2</td>
<td>29.3</td>
</tr>
<tr>
<td>B2</td>
<td>GPAF 0.2</td>
<td>59.8</td>
<td>26.0</td>
</tr>
<tr>
<td></td>
<td>No GPAF 59</td>
<td>130.2</td>
<td>25.3</td>
</tr>
<tr>
<td>B3</td>
<td>GPAF 2.8</td>
<td>58.0</td>
<td>28.0</td>
</tr>
<tr>
<td></td>
<td>No GPAF 64</td>
<td>132.4</td>
<td>28.6</td>
</tr>
<tr>
<td>B4</td>
<td>GPAF 1.8</td>
<td>44.0</td>
<td>25.0</td>
</tr>
<tr>
<td></td>
<td>No GPAF 51</td>
<td>79.7</td>
<td>29.6</td>
</tr>
</tbody>
</table>

Note: 20% Heave: Free field heave = 75 mm

Fig. 5: Deformation of central beams B1 to B4 due to heave and shrinkage

As can be seen in Table 2, the use of the GPAF system significantly reduced the maximum negative bending moments of all beams, but slightly reduced the maximum positive bending moments. For example, the maximum negative and positive moments of beam B1 are 81.2 and 29.3 kN.m, respectively, for the case without the GPAF system, whereas these values are reduced to 44.6 and 23.0 kN.m, respectively, for the case with the GPAF system.

The practical implication of the above results is that the use of the GPAF system for light-weight structures can significantly reduce the superstructure damage induced by reactive soils, leading to immense savings on the cost of structural repairs and ongoing maintenance.

5. SUMMARY AND CONCLUSIONS

This paper presented results from 3D FEM analyses of the granular pile-anchor foundation (GPAF) system as a plausible foundation solution for light-weight structures built on reactive soils. The paper investigated the superstructure response of two-story, four-bay frame building to the ground heave/shrinkage induced by reactive soils.

The results indicate that the effect of the GPAF system in reducing the vertical displacement and angular distortion induced by soil heave are quite significant. It was shown that the maximum vertical displacement of 6.7 mm that is developed at the top beams of the central frame in the case of no GPAF has been totally arrested by the GPAF system, and no heave induced vertical displacement is produced. It was also shown that the GPAF system reduced the maximum angular distortion of the top beams dramatically. In accordance with this, the GPAF system is found to reduce the maximum negative and positive bending moments of the top beams by 56% and 21%, respectively, compared with the maximum negative and positive bending moments produced in the case of no GPAF system. It was also observed that the resistance to shrinkage is improved immensely when the GPAF system is used. The maximum settlement induced by shrinkage for the top beams of the central frame is reduced by 75% compared with the case of no GPAF system.

The above results conclude that the GPAF system is a promising foundation technique that can be potentially used to reduce the detrimental impacts of reactive soils under both heave and shrinkage conditions.
REFERENCES


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